

21. A coil of 200 turns and area 0.20 m^2 is rotated at half a revolution per second and is placed in uniform magnetic field of 0.01 T perpendicular to axis of rotation of the coil. The maximum voltage generated in the coil is $\frac{2\pi}{\beta}$ volt. The value of β is _____.
22. In an ac circuit, the instantaneous current is zero, when the instantaneous voltage is maximum. In this case, the source may be connected to :
A. pure inductor.
B. pure capacitor.
C. pure resistor.
D. combination of an inductor and capacitor.
Choose the correct answer from the options given below :
(1) A, B and C only (2) B, C and D only
(3) A and B only (4) A, B and D only
23. A alternating current at any instant is given by $i = \left[6 + \sqrt{56} \sin \left(100\pi t + \frac{\pi}{3} \right) \right] \text{ A}$. The rms value of the current is _____ A.

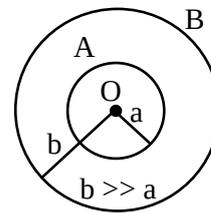
24. Match List I with List II.

	List-I		List-II
A.	Purely capacitive circuit	I.	
B.	Purely inductive circuit	II.	
C.	LCR series at resonance	III.	
D.	LCR series circuit	IV.	

Choose the correct answer from the options given below :

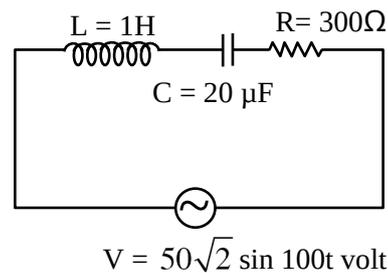
- (1) A-I, B-IV, C-III, D-II
(2) A-IV, B-I, C-III, D-II
(3) A-IV, B-I, C-II, D-III
(4) A-I, B-IV, C-II, D-III

25. A rod of length 60 cm rotates with a uniform angular velocity 20 rad s^{-1} about its perpendicular bisector, in a uniform magnetic field 0.5 T . The direction of magnetic field is parallel to the axis of rotation. The potential difference between the two ends of the rod is _____ V.
26. Two conducting circular loops A and B are placed in the same plane with their centres coinciding as shown in figure. The mutual inductance between them is:



- (1) $\frac{\infty_0 \pi a^2}{2b}$ (2) $\frac{\infty_0}{2\pi} \cdot \frac{b^2}{a}$
(3) $\frac{\infty_0 \pi b^2}{2a}$ (4) $\frac{\infty_0}{2\pi} \cdot \frac{a^2}{b}$

27. An ac source is connected in given series LCR circuit. The rms potential difference across the capacitor of $20 \mu\text{F}$ is V.

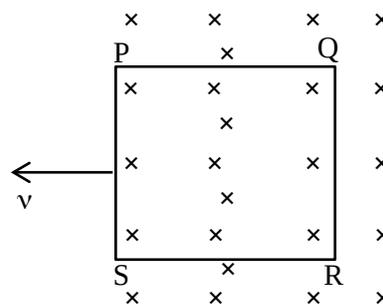


28. A series LCR circuit is subjected to an AC signal of 200 V , 50 Hz . If the voltage across the inductor ($L = 10 \text{ mH}$) is 31.4 V , then the current in this circuit is _____ :
- (1) 68 A (2) 63 A
(3) 10 A (4) 10 mA

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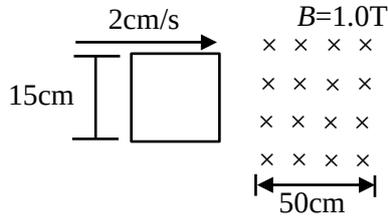
29. The current in an inductor is given by $I = (3t + 8)$ where t is in second. The magnitude of induced emf produced in the inductor is 12 mV. The self-inductance of the inductor _____ mH.
30. Given below are two statements :
Statement I : In an LCR series circuit, current is maximum at resonance.
Statement II : Current in a purely resistive circuit can never be less than that in a series LCR circuit when connected to same voltage source. In the light of the above statements, choose the **correct** from the options given below :
 (1) Statement I is true but Statement II is false
 (2) Statement I is false but Statement II is true
 (3) Both Statement I and Statement II are true
 (4) Both Statement I and Statement II are false
31. When a dc voltage of 100V is applied to an inductor, a dc current of 5A flows through it. When an ac voltage of 200V peak value is connected to inductor, its inductive reactance is found to be $20\sqrt{3} \Omega$. The power dissipated in the circuit is _____ W.
32. In a coil, the current changes form -2 A to $+2$ A in 0.2 s and induces an emf of 0.1 V. The self-inductance of the coil is :
 (1) 5 mH (2) 1 mH
 (3) 2.5 mH (4) 4 mH
33. For a given series LCR circuit it is found that maximum current is drawn when value of variable capacitance is 2.5 nF. If resistance of 200Ω and 100 mH inductor is being used in the given circuit. The frequency of ac source is _____ $\times 10^3$ Hz. (given $\pi^2 = 10$)
34. A LCR circuit is at resonance for a capacitor C, inductance L and resistance R. Now the value of resistance is halved keeping all other parameters same. The current amplitude at resonance will be now:
 (1) Zero (2) double
 (3) same (4) halved

35. A square loop PQRS having 10 turns, area $3.6 \times 10^{-3} \text{ m}^2$ and resistance 100Ω is slowly and uniformly being pulled out of a uniform magnetic field of magnitude $B = 0.5$ T as shown. Work done in pulling the loop out of the field in 1.0 s is _____ $\times 10^6$ J.



36. A coil of negligible resistance is connected in series with 90Ω resistor across 120 V, 60 Hz supply. A voltmeter reads 36 V across resistance. Inductance of the coil is :
 (1) 0.76 H (2) 2.86 H
 (3) 0.286 H (4) 0.91 H
37. A bulb and a capacitor are connected in series across an ac supply. A dielectric is then placed between the plates of the capacitor. The glow of the bulb:
 (1) increases (2) remains same
 (3) becomes zero (4) decreases
38. An alternating emf $E = 110 \sqrt{2} \sin 100t$ volt is applied to a capacitor of $2\mu\text{F}$, the rms value of current in the circuit is mA.
39. When a coil is connected across a 20 V dc supply, it draws a current of 5 A. When it is connected across 20 V, 50 Hz ac supply, it draws a current of 4 A. The self inductance of the coil is _____ mH. (Take $\pi = 3$)

40. A square loop of side 15 cm being moved towards right at a constant speed of 2 cm/s as shown in figure. The front edge enters the 50 cm wide magnetic field at $t = 0$. The value of induced emf in the loop at $t = 10$ s will be :



- (1) 0.3 mV (2) 4.5 mV
(3) zero (4) 3 mV

41. A capacitor of reactance $4\sqrt{3}\Omega$ and a resistor of resistance 4Ω are connected in series with an ac source of peak value $8\sqrt{2}$ V. The power dissipation in the circuit isW.

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SOLUTIONS

1. **Ans. (3)**

Sol. Average emf = $\frac{\text{Change in flux}}{\text{Time}} = -\frac{\Delta \phi}{\Delta t}$
 $= -\frac{0 - (4 \cdot (2.5 \cdot 2) \cos 60^\circ)}{10} = +1\text{V}$

2. **Ans. (2)**

Sol. $\phi = Mi = Mi_0 \sin \omega t$
 EMF = $-M \frac{di}{dt} = -0.002(i_0 \omega \cos \omega t)$
 EMF_{max} = $i_0 \omega (0.002) = (5)(50\pi)(0.002)$

EMF_{max} = $\frac{\pi}{2} \text{V}$

3. **Ans. (3)**

Sol. $\frac{V_1}{V_2} = \frac{N_1}{N_2}; \frac{230}{V_2} = \frac{10}{1}$
 $V_2 = 23\text{V}$

Power consumed = $\frac{V_2^2}{R}$
 $= \frac{23 \cdot 23}{46} = 11.5 \text{W}$

4. **Ans. (1)**

Sol. $X_C = \frac{1}{\omega C} = \frac{\pi}{2\pi \cdot 50 \cdot 10^{-3}} = 10\Omega$

$X_L = \omega L = 2\pi \cdot 50 \cdot \frac{100}{\pi} \cdot 10^{-3}$
 $= 10\Omega$

∴ $X_C = X_L$, Hence, circuit is in resonance

∴ power factor = $\frac{R}{Z} = \frac{R}{R} = 1$

5. **Ans. (2)**

Sol. By energy conservation

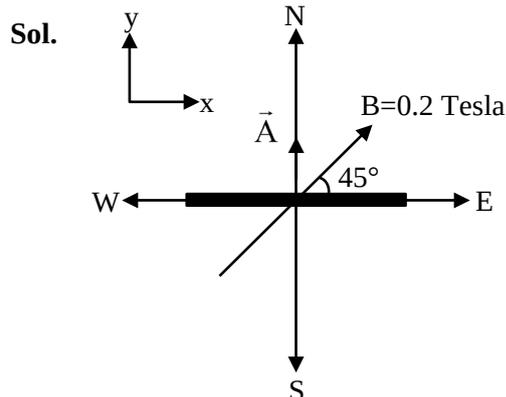
$\frac{1}{2} CV^2 = \frac{1}{2} LI_{\text{max}}^2$

$I_{\text{max}} = \sqrt{\frac{C}{L}} V$

$= \sqrt{\frac{100 \cdot 10^{-6}}{6.4 \cdot 10^{-3}}} \cdot 12$

$= \frac{12}{8} = \frac{3}{2} = 1.5 \text{A}$

6. **Ans. (2)**



$A = (0.1)^2 \hat{j}$

$B = \frac{0.2}{\sqrt{2}} \hat{i} + \frac{0.2}{\sqrt{2}} \hat{j}$

Magnitude of induced emf

$e = \frac{\Delta \phi}{\Delta t} = \frac{B \cdot A \theta}{1} = \sqrt{2} \cdot 10^{-3} \text{V}$

7. **Ans. (3)**

Sol. $P_{\text{avg}} = V_{\text{rms}} I_{\text{rms}} \cos(\Delta \phi)$
 $= \frac{100}{\sqrt{2}} \cdot \frac{100 \cdot 10^{-3}}{\sqrt{2}} \cdot \cos\left(\frac{\pi}{3}\right)$
 $= \frac{10^4}{2} \cdot \frac{1}{2} \cdot 10^{-3} = \frac{10}{4} = 2.5\text{W}$

8. **Ans. (3)**

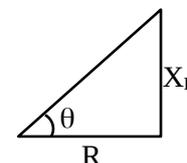
Sol. $B_H = 0.60 \times 10^{-4} \text{Wb/m}^2$
 Induced emf $e = B_H v \ell$
 $= 0.60 \times 10^{-4} \times 10 \times 5 = 3 \times 10^{-3} \text{V}$

9. **Ans. (1)**

Sol. $\frac{\epsilon_1}{\epsilon_2} = \frac{N_1}{N_2} = \frac{100}{10} \Rightarrow \epsilon_2 = 22 \text{V}$
 $I = \frac{22}{22 \cdot 10^3} = 1\text{mA}, V_0 = 7\text{V}$

10. **Ans. (3)**

Sol. $E = 25 \sin(1000 t)$
 $\cos \theta = \frac{1}{\sqrt{2}}$
 LR circuit
 Initially
 $\frac{R}{\omega_1 L} = \frac{1}{\tan \theta} = \frac{1}{\tan 45^\circ} = 1$
 $X_L = \omega_1 L$
 $\omega_2 = 2\omega_1$, given
 $\tan \theta' = \frac{\omega_2 L}{R} = \frac{2\omega_1 L}{R}$
 $\tan \theta' = 2$
 $\cos \theta' = \frac{1}{\sqrt{5}}$



11. Ans. (2)
Sol. Rising half to peak

$$t = T/6$$

$$t = \frac{2\pi}{6\omega} = \frac{\pi}{3\omega} = \frac{\pi}{300\pi} = \frac{1}{300} = 3.33\text{ms}$$

12. Ans. (45)
Sol. $P_i = 2300 \times 5 \text{ watt}$

$$P_0 = 2300 \times 5 \times 0.9 = 230 \times I_2$$

$$I_2 = 45\text{A}$$

13. Ans. (2)
Sol. $\epsilon = N \left(\frac{\Delta \phi}{\Delta t} \right); \Delta \phi = (\Delta B)A$

$$B_i = 5000 \text{ T}, B_f = 3000 \text{ T}$$

$$d = 0.02 \text{ m}$$

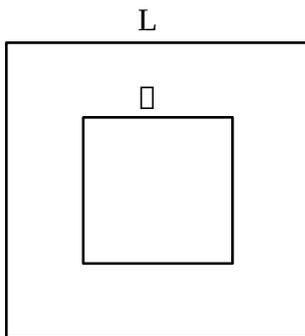
$$r = 0.01 \text{ m}$$

$$\Delta \phi = (\Delta B)A$$

$$= (2000)\pi(0.01)^2 = 0.2\pi$$

$$\epsilon = N \left(\frac{\Delta \phi}{\Delta t} \right) \Rightarrow 22 = N \left(\frac{0.2\pi}{2} \right)$$

$$N = 70$$

14. Ans. (128)
Sol.


Flux linkage for inner loop.

$$\phi = B_{\text{center}} \cdot \square^2$$

$$= 4 \cdot \frac{\infty_0 i}{4\pi \frac{L}{2}} (\sin 45 + \sin 45) \square^2$$

$$\phi = 2\sqrt{2} \frac{\infty_0 i}{\pi L} \square^2$$

$$M = \frac{\phi}{i} = \frac{2\sqrt{2}\infty_0 \square^2}{\pi L} = 2\sqrt{2} \frac{\infty_0}{\pi}$$

$$= 2\sqrt{2} \frac{4\pi}{\pi} \cdot 10^{-7}$$

$$= 8\sqrt{2} \cdot 10^{-7} \text{ H}$$

$$= \sqrt{128} \cdot 10^{-7} \text{ H}, x = 128$$

15. Ans. (4)
Sol. $\langle P \rangle = IV \cos \phi$

$$= \frac{20}{\sqrt{2}} \cdot \frac{10}{\sqrt{2}} \cdot \cos 60^\circ = 50 \text{ W}$$

16. Ans. (4)

$$\begin{aligned} \text{Sol. } I &= \frac{V}{X_C} \\ &= 230 \times 300 \times 200 \times 10^{-12} \\ &= 13.8 \mu\text{A} \end{aligned}$$

17. Ans. (2)

$$\text{Sol. } \epsilon = - \left(\frac{d\phi}{dt} \right) = 10t - 36$$

$$\text{at } t = 2, \epsilon = 16 \text{ V}$$

$$i = \frac{\epsilon}{R} = \frac{16}{8} = 2 \text{ A}$$

18. Ans. (3)
Sol. $\omega' = \omega$

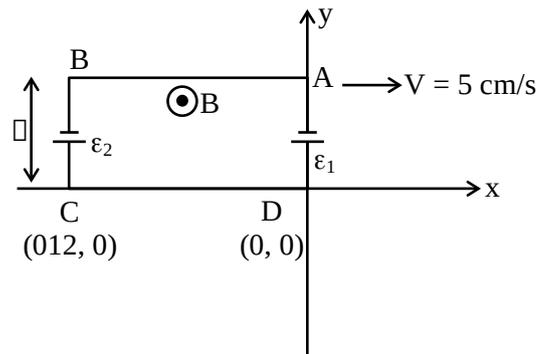
$$\frac{1}{\sqrt{L'C'}} = \frac{1}{\sqrt{LC}}$$

$$\therefore L'C' = LC$$

$$L'(4C) = LC$$

$$L' = \frac{L}{4}$$

$$\therefore \text{Inductance must be decreased by } \frac{3L}{4}$$

19. Ans. (216)
Sol.

 B_0 is the magnetic field at origin

$$\frac{dB}{dx} = \frac{10^{-3}}{10^{-2}}$$

$$\int_{B_0}^B dB = - \int_0^x 10^{-1} dx$$

$$B - B_0 = -10^{-1}x$$

$$B = \left(B_0 - \frac{x}{10} \right)$$

Motional emf in AB = 0

Motional emf in CD = 0

 Motional emf in AD = $\epsilon_1 = B_0 \square$

Magnetic field on rod BC B

$$= \left(B_0 - \frac{(-12 \cdot 10^{-2})}{10} \right)$$

 Motional emf in BC = ϵ_2

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$$= \left(B_0 + \frac{12 \cdot 10^{-2}}{10} \right) \square \cdot \mathbf{v}$$

$$\epsilon_{eq} = \epsilon_2 - \epsilon_1 = 300 \times 10^{-7} \text{ V}$$

For time variation

$$(\epsilon_{eq})' = A \frac{dB}{dt} = 60 \times 10^{-7} \text{ V}$$

$$(\epsilon_{eq})_{net} = \epsilon_{eq} + (\epsilon_{eq})' = 360 \times 10^{-7} \text{ V}$$

$$\text{Power} = \frac{(\epsilon_{eq})_{net}^2}{R} = 216 \times 10^{-9} \text{ W}$$

20. Ans. (2)

Sol. Efficiency = $\frac{E_{sS}}{E_{pP}}$

$$0.8 = \frac{240I_s}{4000}$$

$$I_s = \frac{3200}{240} = 13.33A$$

21. Ans. (5)

Sol. $\phi = NAB \cos(\omega t)$

$$\epsilon = -\frac{d\phi}{dt} = NAB\omega \sin(\omega t)$$

$$\epsilon_{max} = NAB\omega$$

$$= 200 \times 0.2 \times 0.01 \times \pi$$

$$= \frac{4\pi}{10} = \frac{2\pi}{5} \text{ volt}$$

22. Ans. (4)

Sol. This is possible when phase difference is $\frac{\pi}{2}$

between current and voltage so correct answer will be (4)

23. Ans. (8)

Sol. $I_{rms} = \sqrt{\frac{\int i^2 dt}{\int dt}}$

$$I_{rms} = \sqrt{(6)^2 + \frac{(\sqrt{56})^2}{2}}$$

$$= \sqrt{36 + 28} = \sqrt{64} = 8A$$

24. Ans. (4)

Sol. A – V lags by 90° from I hence option (I) is correct.

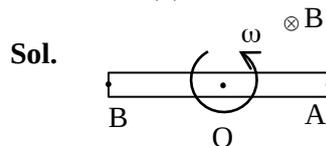
B – V lead by 90° from I hence option (IV) is correct

C – In LCR resonance $X_L = X_C$. Hence circuit is purely resistive so option (II) is correct

D – In LCR series V is at some angle from I hence (III) is correct

Hence option (4) is correct.

25. Ans. (0)



$$\therefore V_0 - V_A = \frac{B\omega l^2}{2}$$

$$V_0 - V_B = \frac{B\omega l^2}{2}$$

$$\therefore V_A = V_B$$

$$\therefore V_A - V_B = 0$$

26. Ans. (1)

Sol. $\phi = Mi = BA$

$$\Rightarrow Mi = \frac{\infty_0 i}{2b} \pi a^2$$

$$\therefore M = \frac{\infty_0 \pi a^2}{2b}$$

27. Ans. (50)

Sol. $X_L = \omega L = 100 \times 1 = 100\Omega$

$$X_C = \frac{1}{\omega C} = \frac{1}{100 \cdot 20 \cdot 10^{-6}} = 500\Omega$$

$$Z = \sqrt{(X_L - X_C)^2 + R^2}$$

$$\sqrt{(100 - 500)^2 + 300^2}$$

$$Z = 500\Omega$$

$$i_{rms} = \frac{V_{rms}}{Z} = \frac{50}{500} = 0.1A$$

rms voltage across capacitor

$$V_{rms} = X_C i_{rms}$$

$$= 500 \times 0.1 = 50V$$

28. Ans. (3)

Sol. Voltage across inductor $V_L = IX_L$

$$31.4 = I[L\omega]$$

$$31.4 = I[L(2\pi f)]$$

$$31.4 = I[10 \times 10^{-3}(2 \times 3.14) \times 50]$$

$$\Rightarrow I = 10 \text{ A}$$

29. Ans. (4)

Sol. $I = 3t + 8$

$$\epsilon = 12 \text{ mV}$$

$$|\epsilon| = L \left| \frac{dI}{dt} \right|$$

$$12 = L \times 3$$

$$L = 4 \text{ mH}$$

30. **Ans. (3)**

Sol. Statement-I

$$I_m = \frac{V_m}{\sqrt{R^2 + (X_L - X_C)^2}} \text{ at resonance } X_L = X_C$$

$$\text{Thus, } I_m = \frac{V_m}{R}$$

∴ Impedance is minimum therefore I is maximum at resonance.

Statement-II

$$I = \left(\frac{V}{R}\right) \text{ in purely resistive circuit.}$$

31. **Ans. (250)**

Sol. For DC voltage

$$R = \frac{V}{I} = \frac{100}{5} = 20 \Omega$$

for AC voltage

$$X_L = 20\sqrt{3} \Omega$$

$$R = 20 \Omega$$

$$Z = \sqrt{X_L^2 + R^2} = \sqrt{3 \cdot 400 + 400} = 40 \Omega$$

$$\text{Power} = i_{\text{rms}}^2 R$$

$$= \left(\frac{V_{\text{rms}}}{Z}\right)^2 \cdot R = \left(\frac{200}{40}\right)^2 \cdot 20 = 250W$$

32. **Ans. (1)**

Sol. $(\text{Emf})_{\text{induced}} = -L \frac{di}{dt}$

In magnitude form,

$$|\text{Emf}_{\text{ind}}| = \left|(-)L \frac{di}{dt}\right|$$

$$\Rightarrow 0.1 = \frac{(L)[+2 - (-2)]}{0.2}$$

$$\Rightarrow \boxed{L = \frac{0.1 \cdot 0.2}{4} = 5\text{mH}}$$

33. **Ans. (10)**

Sol. for maximum current, circuit must be in resonance.

$$f_0 = \frac{1}{2\pi\sqrt{L \cdot C}}$$

$$f_0 = \frac{1}{2\pi\sqrt{100 \cdot 10^{-3} \cdot 2.5 \cdot 10^{-9}}}$$

$$= \frac{1}{2\pi\sqrt{25 \cdot 10^{-11}}}$$

$$= \frac{1}{2\pi \cdot 5} \cdot 10^5 \cdot \sqrt{10} \text{ Hz}$$

$$= \frac{100}{10} \cdot 10^3 \text{ Hz}; f_0 = 10 \times 10^3 \text{ Hz}$$

34. **Ans. (2)**

Sol. In resonance $Z = R$

$$I = \frac{V}{R}$$

$R \rightarrow \text{halved} \Rightarrow I \rightarrow 2I$

I becomes doubled.

35. **Ans. (3)**

Sol. $\epsilon = NBLv$

$$i = \frac{\epsilon}{R} = \frac{NBLv}{R}$$

$$F = N(iBL) = \frac{N^2 B^2 v^2}{R}$$

$$W = F \cdot \Delta x = \frac{N^2 B^2 v^2}{R} \left(\frac{\Delta x}{t}\right)$$

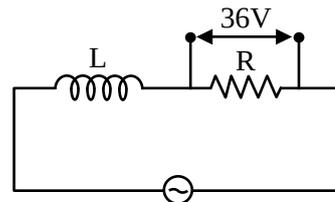
$$A = \Delta x^2$$

$$W = \frac{(10 \cdot 10)(0.5)^2 \cdot (3.6 \cdot 10^{-3})^2}{100 \cdot 1}$$

$$W = 3.24 \times 10^{-6} \text{ J}$$

36. **Ans. (1)**

Sol.



$$36 = I_{\text{rms}} R$$

$$36 = \frac{120}{\sqrt{X_L^2 + R^2}} \cdot R$$

$$R = 90 \Omega \Rightarrow 36 = \frac{120 \cdot 90}{\sqrt{X_L^2 + 90^2}}$$

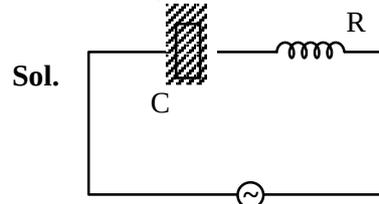
$$\sqrt{X_L^2 + 90^2} = 300; X_L^2 = 81900$$

$$X_L = 286.18$$

$$\omega L = 286.18$$

$$L = \frac{286.18}{376.8}; L = 0.76 \text{ H}$$

37. **Ans. (1)**



$$Z = \sqrt{R^2 + X_C^2} \text{ \& } X_C = \frac{1}{\omega C}$$

due to dielectric

$C \uparrow \Rightarrow X_C \downarrow \Rightarrow Z \downarrow$

So, current increases & thus bulb will glow more brighter.

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38. Ans. (22)

Sol. $C = 2\mu\text{f}$; $E = 110\sqrt{2} \sin(100t)$

$$X_C = \frac{1}{\omega C} = \frac{1}{100 \cdot 2 \cdot 10^6}$$

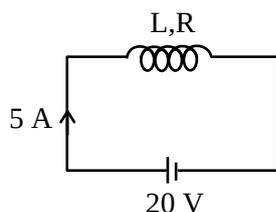
$$= \frac{10000}{2} = 5000\Omega$$

$$i_0 = \frac{110\sqrt{2}}{5000}; i_{\text{rms}} = \frac{110\sqrt{2}}{5000\sqrt{2}}$$

$$= \frac{110}{5} \text{mA} = 22 \text{mA}$$

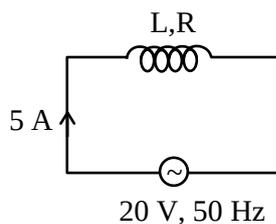
39. Ans. (10)

Sol. Case-I:



$$i = \frac{20}{R} \Rightarrow R = 4\Omega$$

Case-II:



$$i = \frac{20}{Z}$$

$$4 = \frac{20}{\sqrt{R^2 + X_L^2}} \Rightarrow \sqrt{R^2 + X_L^2} = 5$$

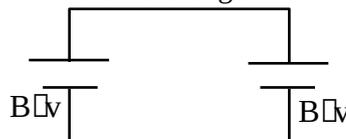
$$R^2 + X_L^2 = 25 \Rightarrow X_L = 3\Omega$$

$$L = \frac{3}{2\pi} = \frac{1}{2 \cdot 50} = \frac{1000}{100} \text{mH}$$

$$L = 10 \text{mH}$$

40. Ans. (3)

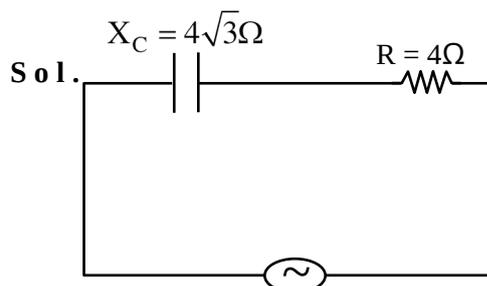
Sol. At $t = 10$ sec complete loop is in magnetic field therefore no change in flux



$$e = \frac{d\phi}{dt} = 0$$

$e = 0$ for complete loop

41. Ans. (4)



$$Z = \sqrt{R^2 + X_L^2}$$

$$Z = \sqrt{4^2 + (4\sqrt{3})^2} = 8\Omega$$

$$V_{\text{rms}} = \frac{V}{\sqrt{2}} = \frac{8\sqrt{2}}{\sqrt{2}} = (8\text{V})$$

$$I_{\text{rms}} = \frac{V_{\text{rms}}}{Z} = \frac{8}{8} = 1\text{A}$$

$$\text{Power dissipated} = I_{\text{rms}}^2 \times R = 1 \times 4 = (4\text{W})$$